04IN1023: Introduction to functional programming
Final—Dry run SS 2014
Universität Koblenz-Landau, FB4
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Studiengang □ BSc Inf □ BSc CV □ ............................
Prüfungsversuch □ 1 □ 2 □ 3

Hiermit bestätige ich, dass ich zur Klausur angemeldet und zugelassen bin.
Eine falsche Angabe wird als Täuschungsversuch gewertet.

Unterschrift: ..............................

Korrekturabschnitt

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Exam Manual

1. If you have any questions regarding the following items, please ask them during the dry run. You can ask them during the final or the re-sit as well, but this may be less helpful to you.

2. There are 10 assignments with 0-2 points each. 0 means ‘missing’ or ‘wrong’; 1 means ‘arguably appropriate, but significantly incomplete or incorrect’; 2 means ‘appropriate and essentially complete and correct’. You might get an extra point, if you come up with an exceptionally insightful solution.

3. The exam lasts 1 hours. Thus, one can spend more than 5 min per assignment. All assignments only require very few lines of code: 1–5 in the reference solution. Overly long code may receive a reduced score. If text is required, a 140 chars limit applies.

4. The overall topics for the exam are defined with the dry-run; see the section headers. These topics are maintained for the actual final and the re-sit of the given course edition. The topics may be somewhat different in the next edition. The topics leave, of course, much freedom as to the actual assignment.

5. One should be prepared—systematically—that the text of the assignments relates to the (software) concepts that are listed for each lecture. Definitions of the concepts are never inquired, but basic understanding of the concepts is assumed and crucial for passing the exam.

6. One is advised to establish familiarity with the illustrations given for all concepts. These illustrations are often invoked, perhaps after some modulation, to provide for the exam assignments or to ask code in the assignments.

7. Detailed library knowledge (such as combinators of libraries for parsing or pretty printing) is never assumed; relevant hints would be provided, if libraries are to be used. Familiarity with Haskell’s Prelude, though, is assumed—to the extent it is covered in the lecture.
1 “Simple algorithms”

Define a function that tests whether a given list of ints is sorted (in any order you favor).
 Declare a data type for shapes as follows. One kind of shape is ‘triangle’ described by three points. Each point consists of two ints for the x/y coordinates. Another kind of shape is ‘circle’ described by one point (the centre) and an Int for the radius. Yet another kind of shape is ‘composite’ described by two shapes that are composed in this way.
3 “Local scope”

Consider the following code:

\[
\begin{align*}
f \; x \; y &= g \; y \\
& \text{where} \\
& \quad g \; z = x + z
\end{align*}
\]

Transform the code such that no local scope is used, i.e., the function \(g\) shall be defined at the top-level as opposed to the local scope of \(f\).
4 “Parametric polymorphism”

Define a polymorphic function including its function signature for swapping the two components of a pair.
5  “Higher-order functions”

Define a polymorphic function \( \text{times} \) which repeats the application of a given argument function, as demonstrated with the following example:

\[
\text{> times 22 (+1) 20}
\]

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6 “Monoids”

Why is Float not readily defined to be an instance of the Monoid type class?
*Please, be concise: 140 characters or less.*
7 “Functors”

Consider the following code:

```haskell
-- Sets as lists
data Set a = Set [a]
  deriving Show

-- Construct the empty set
empty :: Set a
empty = Set []

-- Add an element to a set
addTo :: Eq a => a -> Set a -> Set a
addTo x (Set xs) =
  Set $ if elem x xs
    then xs
    else x:xs

-- Functor instance for sets
instance Functor Set
  where
    fmap f (Set xs) = Set (map f xs)
```

The `addTo` function and the functor instance are not perfectly aligned in that an application of `fmap` could lead to a set representation that cannot be possibly reached by a repeated application of `addTo` starting from `empty`. Please explain or give an illustrative sample expression! Please, be concise: 140 characters or less.
8  “Unparsing & parsing”

Remember the two horizontal composition operators for unparsing:

-- Compose horizontally
(<>): Doc → Doc → Doc

-- Compose horizontally with extra space for separation
(<+>): Doc → Doc → Doc

Why is the following definition of the latter in terms of the former possibly problematic?

x <+> y = x <> text " " <> y
Consider the following binary search tree $t$.

![Binary Search Tree Diagram]

Now, assume that 8 is inserted into $t$, resulting in a tree $t'$. Draw the tree $t'$ so that one can see what parts it shares with $t$. 

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9 “Functional data structures”

Many of the standard heap data structures can easily be adapted to a functional setting, including binomial queues \[7, 15\] and leftist heaps \[18, 24\]. In this section, we describe a simple, yet interesting, design known as skew heaps \[32\]. (Non-persistent skew heaps are...
10 “Reasoning”

How would you test the head function for retrieving the head of a list?
*Please, be concise: 140 characters or less.*